

# Sustainability Economics of Groundwater Usage and Management

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## 1. Sustainability concepts

Some representative definitions from the general literature:

*“Sustainable development is development that meets the needs of the present without compromising the ability of future generations to meet their own needs.”*

World Commission on Environment and Development (1987)

*“We summarize the necessary conditions [for sustainable development] as ‘constancy of the natural resource stock’. More strictly, the requirement as for non-negative changes in the stock of natural resources such as ... ground surface waters and their quality, land biomass ... and the waste assimilative capacity of the environment.”*

Pearce, D., E. Barbier, and A. Markandya. *Sustainable Development and Cost-Benefit Analysis*. 1988.

While these definitions likely point us in a useful direction, they can be very limited for quantitative policy analysis:

### “Needs” type definitions:

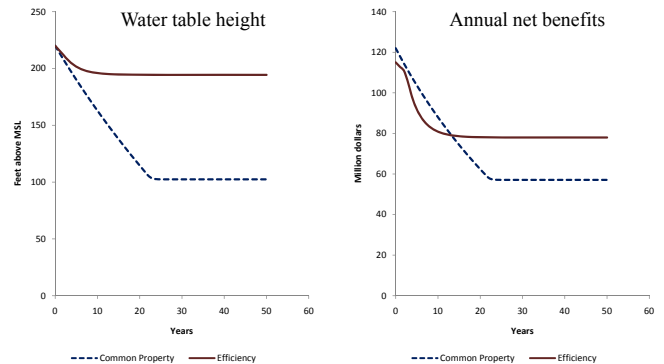
- What are needs?
- Zero-one, all-or-nothing quality.

### “Natural stock” definitions:

- Population and economic growth must inevitably draw down at least some natural resource stocks.
- How does one calculate the stock to maintain?
- Substitution possibilities.
- Nonrenewable resources.
- Natural capital is generating rents and incomes, this isn’t necessarily consumption.
- Confuses means with ends.

Many studies don’t define sustainability at all.

## Groundwater economics: partial equilibrium analysis



### Dilemmas:

- Drawing down natural resource stocks from an initial full level is inevitable. This means declining incomes for at least some time interval.
- An infinite number of steady-states, so how does one choose?
- Focusing on the resource alone ignores other possibilities for achieving end goals.

### Way out:

What’s coming off resource stock is income, not consumption, so investment can at least partially compensate for natural resource scarcity.

Consider socioeconomic and environmental systems jointly.

## Environmental macro-economics literature

*Capital/resource economy*  
 Dasgupta and Heal (1979)

*Can economies physically continue to grow with nonrenewable resources?*  
 Solow (1974), Stiglitz (1974)

*Will markets result in economic growth with nonrenewable resources?*  
 Mourmouras

*Social choice and sustainability*  
 Asheim (2001)

*What about PV-optimality?*  
 Pezzey

*Sustainability Policy:*  
 Hartwick (1977), Solow (1974).

**Sustainability: a proposed definition and framework from the environmental macro-economics literature.**

**Sustainability =**

Intertemporal Efficiency [*Pareto-optimality*]

Intergenerational Equity [*Non-declining utility over time*]

**Total capital =**

Physical/human capital [Factories, roads, knowledge]

Natural resource stock [groundwater]

## 2. Model

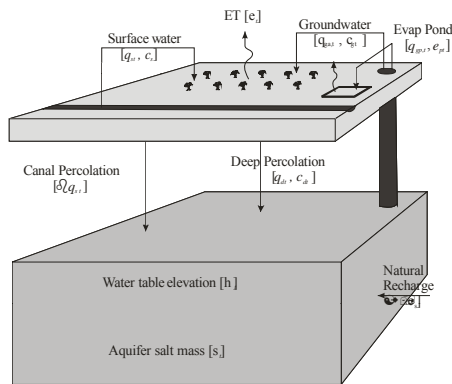
Region with surface water supply and overlying a groundwater aquifer.

Households: consumption and savings/investment.

Production sectors = agriculture + manufacturing.

Kern county agriculture and water data.

U.S. growth data for manufacturing and capital stock data.



### (a) Households

Utility function:

$$U[c(t)] = \text{Log}[c(t)]$$

Household utility depends on annual consumption

*These are one determinant of intertemporal preferences.*

Savings/investment rate =  $\varphi$  (constant rate).

*This is consistent with Solow/Swan neoclassical growth model and U.S. empirical data.*

### (b) Regional output balance equation

Regional output (GDP) can be used for consumption or investment in the capital stock.

- Output balance equation

$$c(t) + \Delta k(t) = q(a,t) + q(m,t) - \gamma(s,t) - \gamma(g,t)$$

- Surface water costs

$$\gamma_{st} = 15.47q_{st} + 1.365q_{st}^2 + 6.239q_{st}^3$$

$$\gamma_{gt} = -22.03 + 84.89q_{gt} - 70.69q_{gt}^2 + 30.79q_{gt}^3$$

- Groundwater pumping costs

$$\gamma_{gt} = \gamma^{pc} q_{gt} + \gamma^e (h^i - h_t) q_{gt} + \frac{\gamma^e q_{gt}^2}{2AS^v}$$

### (c) Agricultural production

Net returns from agriculture:

$$\Pi_t^a = \sum_i \sum_j \pi_{ijt} x_{ijt} \quad \pi_{ijt} = p_j y_{ijt} - \gamma_{ij}$$

Crop yield production function:

$$y_{ijt} = \frac{\bar{y}_{ij}}{1 + \varphi_{1ij} \left( \frac{w_{ijt}}{w_{15ij}} \right)^{\varphi_{2ij}}}$$

Deep percolation production function:

$$d_{ijt} = \alpha_{1ij} + \alpha_{2ij} w_{ijt} + \alpha_{3ij} w_{ijt}^2$$

Water usage:

$$w_{ijt} = w_{ijt}^g + w_{ijt}^s$$

**(d) Manufacturing sector**

Production function:  $\Pi_m = k_t^\beta$

where  $\beta=0.2$  is the capital share.

**(e) Regional water and land usage.**

Surface water:

$$q_{st} = \frac{1}{1-\beta_x} \sum_i \sum_j w_{ijt}^x x_{ijt} \leq \bar{q}_{st}$$

Groundwater extractions:

$$q_{gt} = \sum_i \sum_j w_{ijt}^g x_{ijt}$$

Land constraint:

$$\sum_i \sum_j x_{ijt} \leq \bar{x}$$

**(f) Regional deep percolation and stock dynamics.**

Deep percolation

$$q_{dt} = \sum_i \sum_j d_{ijt} x_{ijt}$$

Equation of motion for water table height:

$$\dot{h}_{t+1} = \bar{h}_t + \frac{1}{AS^y} (\omega + q_{dt} + \beta_s q_{st} - q_{gt})$$

Equation of motion for the capital stock:

$$K_{t+1} = K_t(1 - \delta) + I_t$$

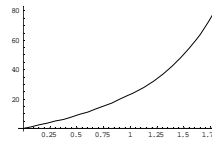
**Kern County, California**

Agricultural production

cotton, tomatoes

evaporation ponds

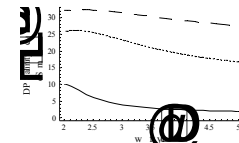
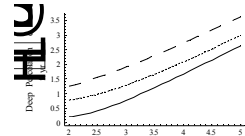
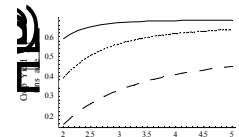
Surface water costs



Aquifer

area = 1.3 10<sup>6</sup> acres, h<sub>top</sub> - h<sub>bottom</sub> = 618 feet  
 specific yield = .13  
 natural recharge = .052 10<sup>6</sup> af/yr

Crop water production functions



— c=1  
 ..... c=10  
 - - - c=20

**U.S. growth data**

Savings/investment rate = 0.2

Capital share = 0.2

Depreciation = .06

**3. Common property usage.**

Unregulated usage

Users are essentially free to use the resource as they desire

Groundwater extractions

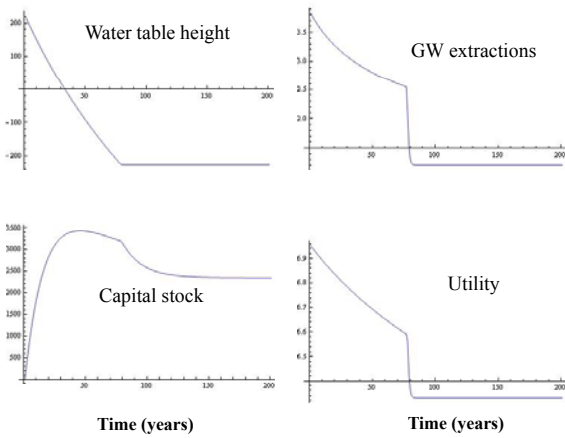
With many users in the basin it is reasonable to assume the following:

- groundwater extractions are chosen to maximize current profits without regard to future levels of the water table level
- deep percolation flows and salt emissions to the aquifer are made as a byproduct of profit-maximization, again no explicit concern for future levels of aquifer hydraulic head or salt concentration

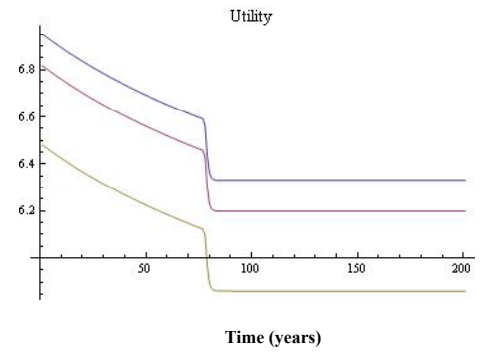
Investment/savings

Neoclassical (Solow-Swan) model: Constant rate of savings/investment consistent with empirical facts.

**Common property usage: Investment rate ( $\phi$ ) = 0.2**



**Common property usage: Investment rate ( $\phi$ ) = {0.2, 0.3, 0.5}**



**4. Present-value optimality (efficiency).**

Present value is defined by

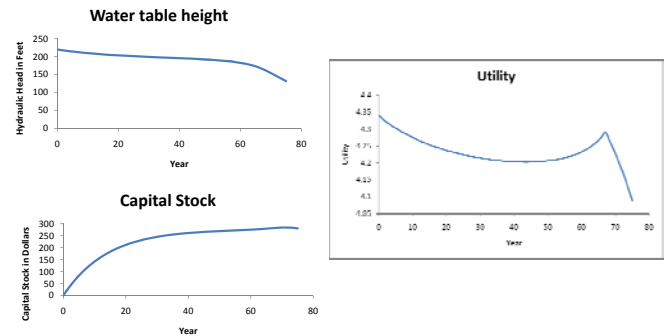
$$W = \sum_{t=1}^T \alpha^t u(c_t)$$

where  $\alpha = 1/(1+\rho)$  is the discount factor, and  $\rho$  is the subjective rate of time preference.

Present-value optimality selects extractions to maximize  $W$  subject to the various definitions, equations and constraints in the model.

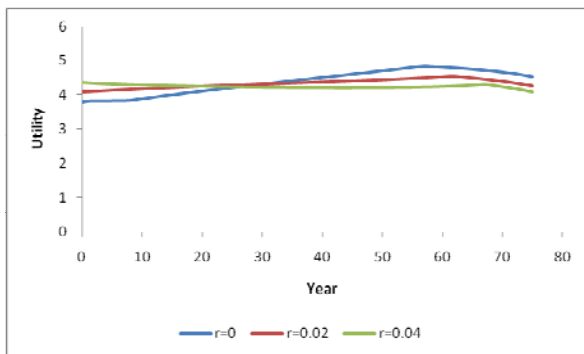
This generates an efficient outcome in terms of Pareto-optimality.

**Efficient extractions.**



**Notes: investment rate ( $\phi$ ) = 0.2**

**Efficient extractions with different social discount rates.**



**5. Sustainability.**

*Market equilibrium (common property) and PV-optimality can lead to declining consumption over some time-frames.*

Sustainability is defined by:

(a) **Efficiency (Pareto-optimality/PV-optimality)**

$$W = \sum_{t=1}^T \alpha^t u(c_t)$$

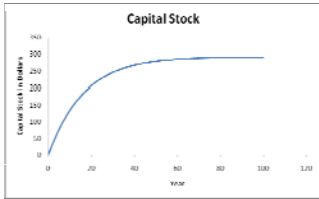
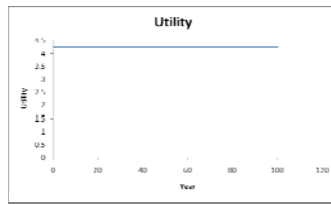
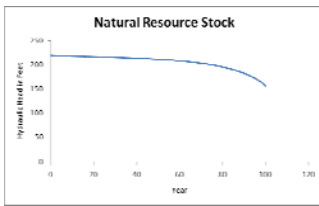
where  $\alpha = 1/(1+\rho)$  is the discount factor, and  $\rho$  is the subjective rate of time preference.

(b) **Equity (non-declining utility over time)**

$$u[c(t)] \leq u[c(t+1)]$$

Select extractions to maximize  $W$  subject to the various definitions, equations and constraints in the model.

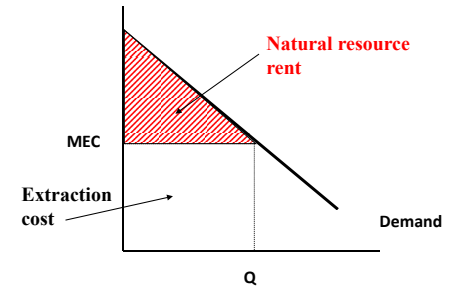
## Sustainable resource extractions



Investment rate ( $\phi$ ) = 0.2, interest rate = .04. Without sustainability, utility is declining over time.

## 6. Hartwick-Solow rule

Resource rents  
( $P - MEC$ )  $Q$ .



If we invest resource rents in capital stock, then we can maintain consumption forever.

Only holds under specialized conditions, but still useful insight.

## 7. Conclusions.

### Concept of sustainability

- We need to define sustainability, otherwise we'll be talking past each other at some point.
- Existing definitions point in useful direction, but can't be basis for quantitative policy analysis.
- Can't just focus on natural resource stock alone, must consider socioeconomic and environmental systems jointly.

### Sustainable groundwater management

Common property (market equilibrium) can lead to declining regional welfare after some point.

PV-optimality as commonly used in economic gw mngt studies doesn't guarantee sustainability either. Reason: this is about efficiency, sustainability also involves equity.

Utility-constraint: some theoretical limitations.

### Future research

Further characterize when sustainability is achieved by the market and PV-optimality.

Improved sustainability criteria.

Scaling issues.

Sustainability policy instruments.